



COMPRESSION BEHAVIOR OF DRY, MOIST AND WET ELASTO-PLASTIC GRANULES

Janett Schmelzer, M. Sc.

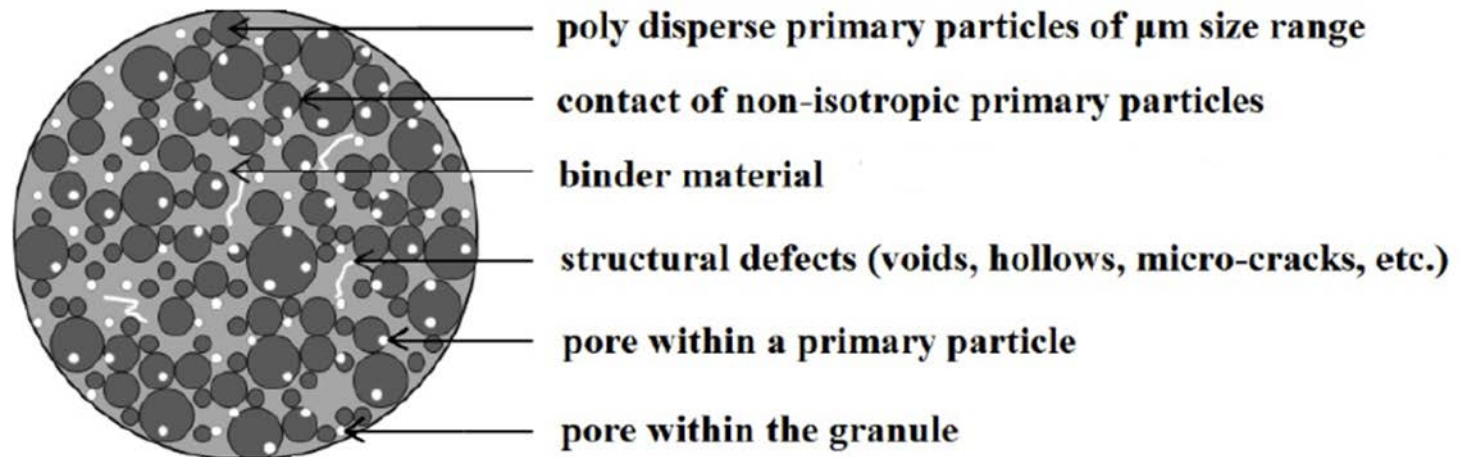
Betreuer der Masterarbeit:

Alexander Russell, M.Sc. , Dr.-Ing. Peter Müller

Jun.-Prof. Dr.-Ing. Manja Krüger, Prof. Dr.-Ing. habil. Jürgen Tomas

Handling of Granular Material

- fine inhomogeneous agglomerates ($d > 100\mu\text{m}$)
- consisting of discrete solid primary particles ($10\ \mu\text{m} < d < 100\ \mu\text{m}$)
- bonded by adhesive forces, liquid or solid bridges



Advantages:

- improved flowability
- reduced dust formation and segregation
- higher bulk density

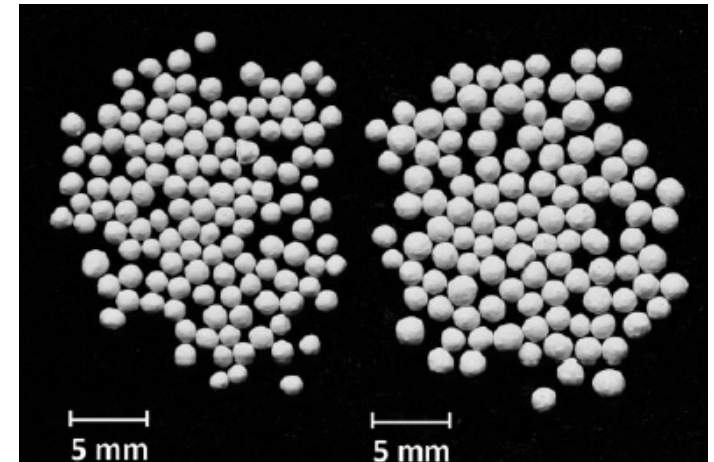
Disadvantages:

- inhomogeneous
- anisotropy
- random shape and size distributions

Test Material – Zeolite 4AK

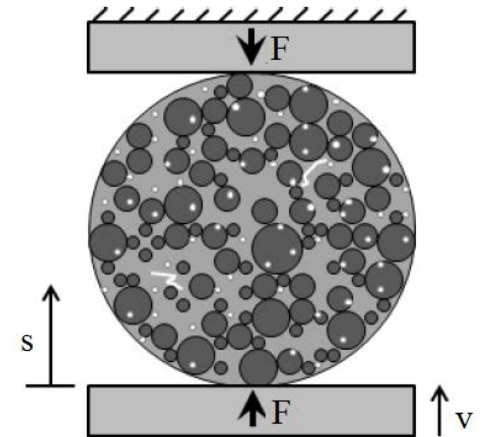
- water-insoluble, arguably spherical and highly hygroscopic granules
- regular pore size with a defined pore diameter of 4 Å (0.4 nm)
- 83% primary particles: $\text{Na}_2\text{O} \cdot \text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2 \cdot n\text{H}_2\text{O}$
- 17% binder material: $(\text{Mg,Al})_2 \cdot \text{Si}_4\text{O}_{10} \cdot (\text{OH}) \cdot 4(\text{H}_2\text{O})$
- mechanical behavior: elasto-plastic deformation until brittle breakage
- adsorber for water and organic liquids

granule size d_{50} in mm	1.75	3.05
sphericity Ψ	0.98	0.98
granule density ρ_g in kg/m^3	1127.9	1102.0
solid density ρ_s in kg/m^3	2290.7	2374.7
porosity ε in %	50.8	53.6
specific surface area S_m in m^2/kg	38.13	44.25

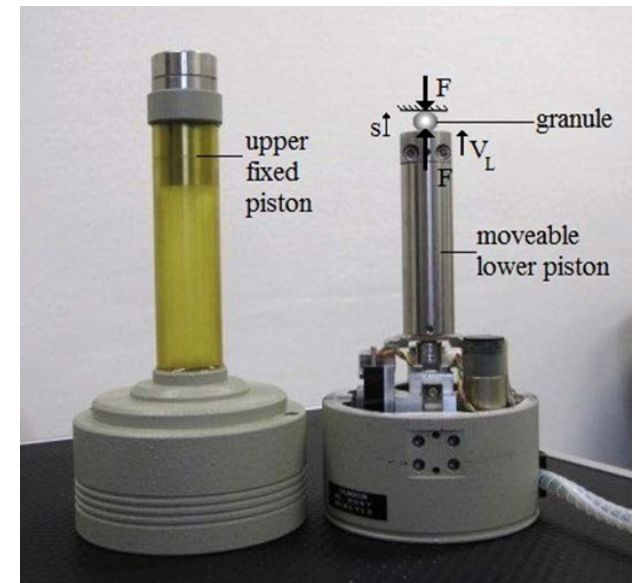


Test Method

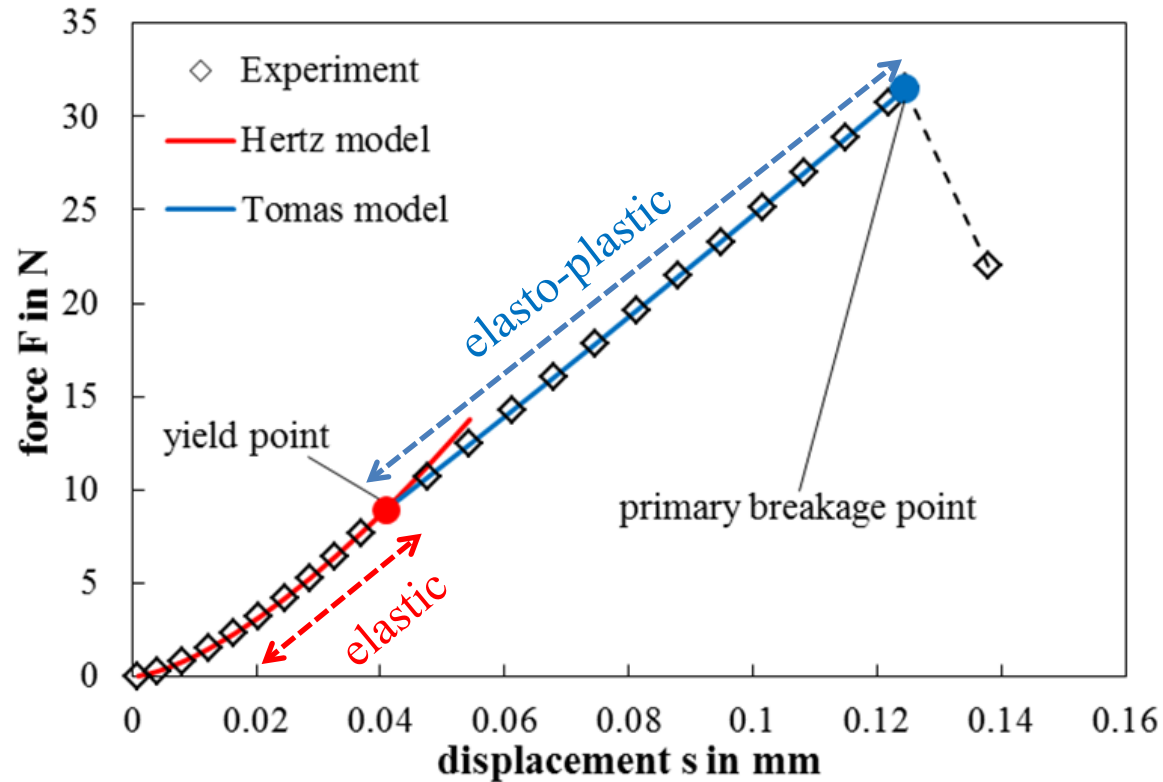
- uniaxial stressing between two flat and rigid contacts
- two test methods:
 - **monotonic loading** until primary breakage
 - **cyclic loading** (until primary breakage) with a load equal to 90% of the mean breakage force of fresh granules



Granule size d_{50} in mm	1.75			3.05		
Loading velocity v in mm/min	0.2	1.5	2.0	0.2	1.5	2.0
Moisture content X_w in $\text{kg}_w/\text{kg}_{DS}$	0.00			0.00		
	0.16			0.14		
	0.45			0.49		



Force-Displacement Behavior



Hertz Model¹

$$F_{\text{el,w-g-w}} = \frac{1}{6} E^* \sqrt{d_1 s^3} = \frac{1}{3} \frac{1}{(1 - \nu_1^2)} E_1 \sqrt{d_1 s^3}$$

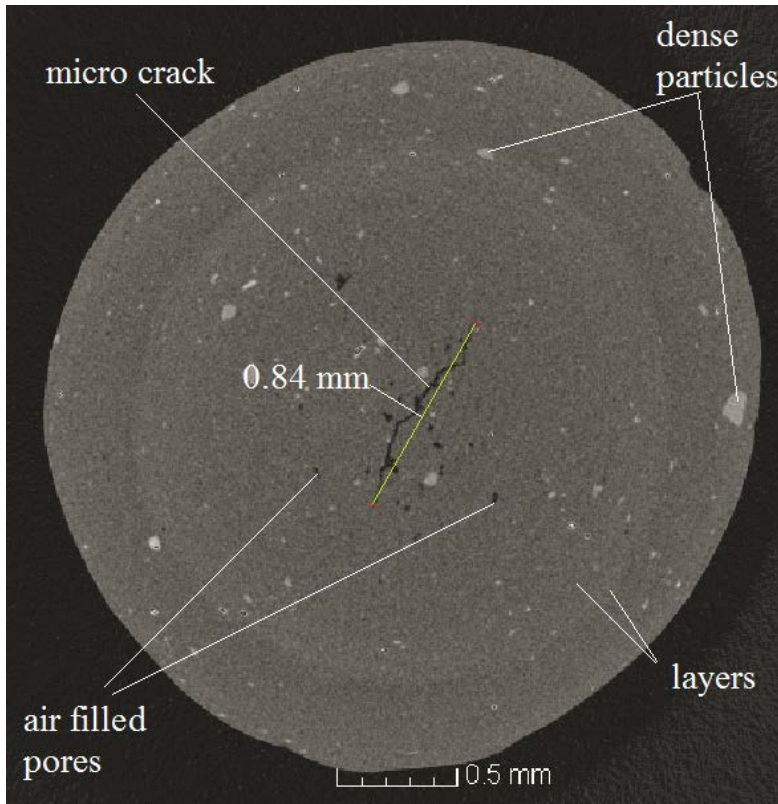
Tomas Model²

$$F_{\text{el-pl,w-g-w}} = \pi \lambda_{\text{el-pl}} R_1 p_y \left(1 - \frac{1}{3} \sqrt[3]{\frac{s_y}{s}} \right) \frac{s}{2}$$

1: Hertz, H., Journal für die reine und angewandte Mathematik 92, 156–171 (1882)

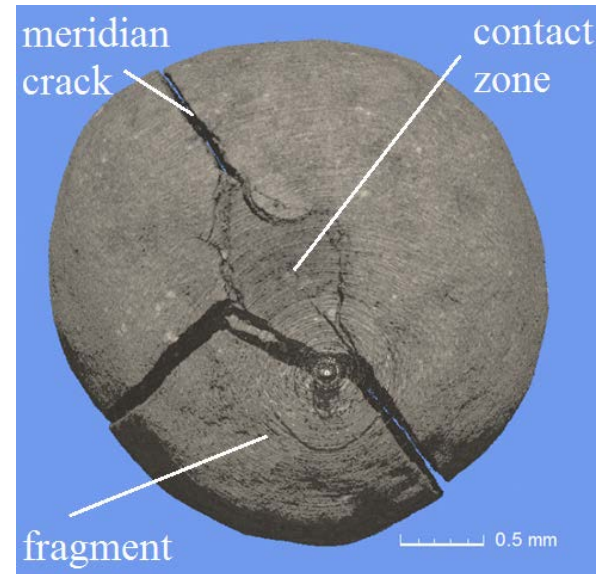
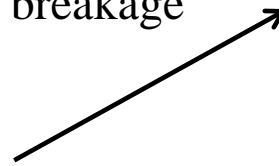
2: Tomas, J., Chem. Eng. Sci. 62, 1997–2010 (2007)

fresh and dry granule:

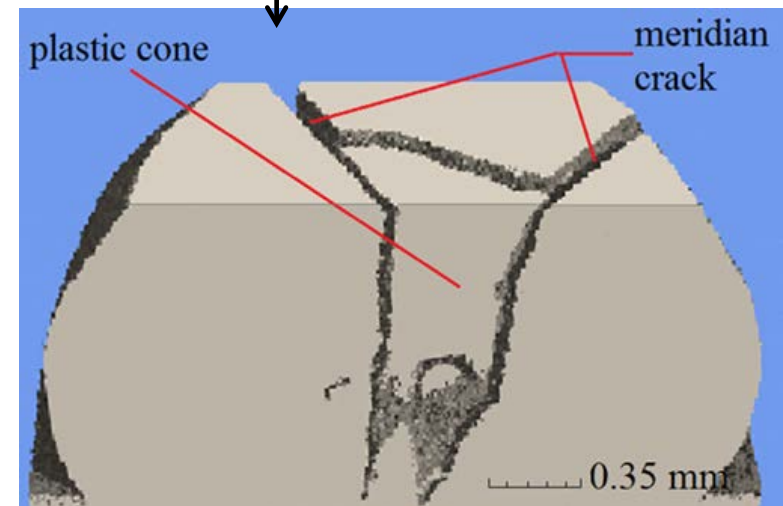


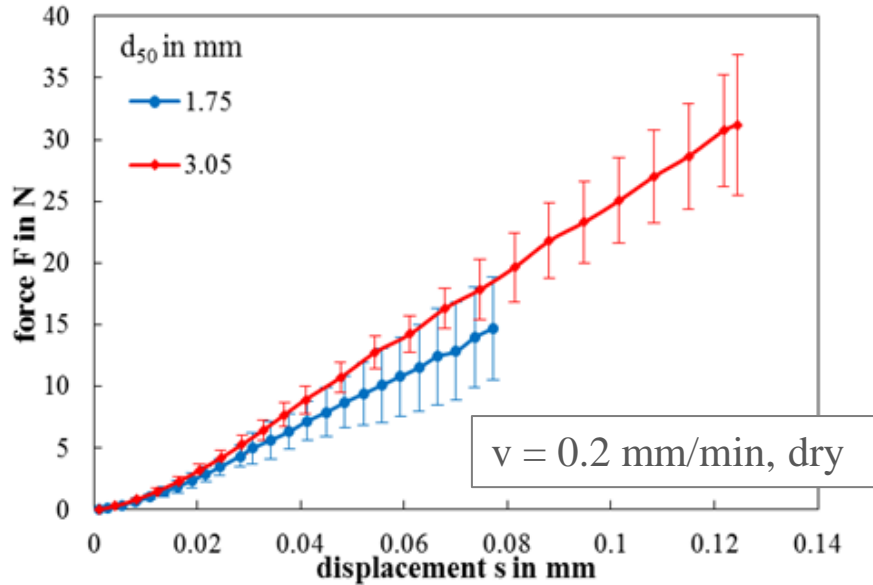
- micro cracks
- air filled pores
- layers
- unknown dense particles

monotonic loading until primary breakage



cross section



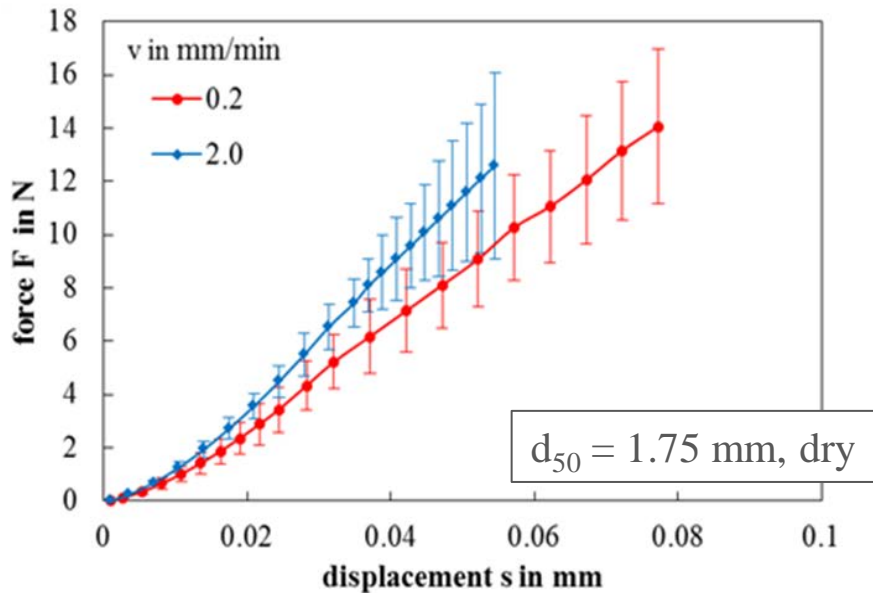


With increasing granule size:

- increase of k_{el} due to the Hertz law

$$k_{el,w-g-w} = \frac{1}{2} \frac{E_1}{(1-\nu_1^2)} \sqrt{d_1 s}$$

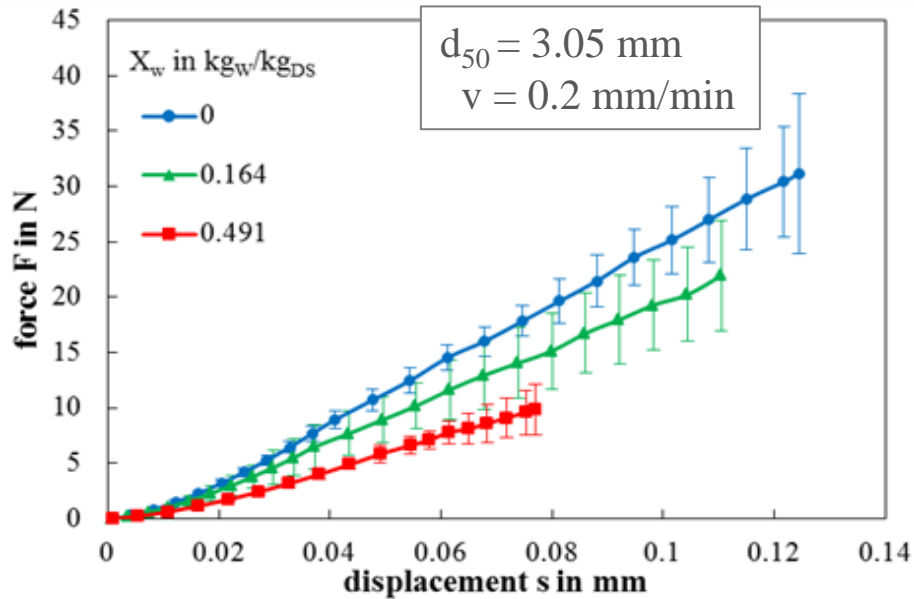
- decrease of E and p_y due to the higher influence of inhomogeneities



With increasing loading velocity:

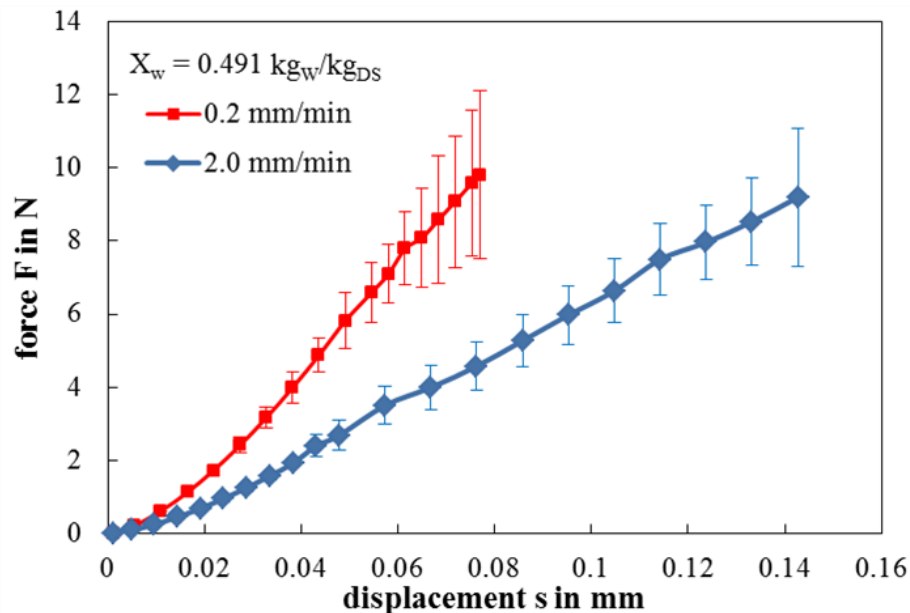
- increase of k_{el} , E and p_y

Material Behavior of Fresh Granules



With increasing moisture content :

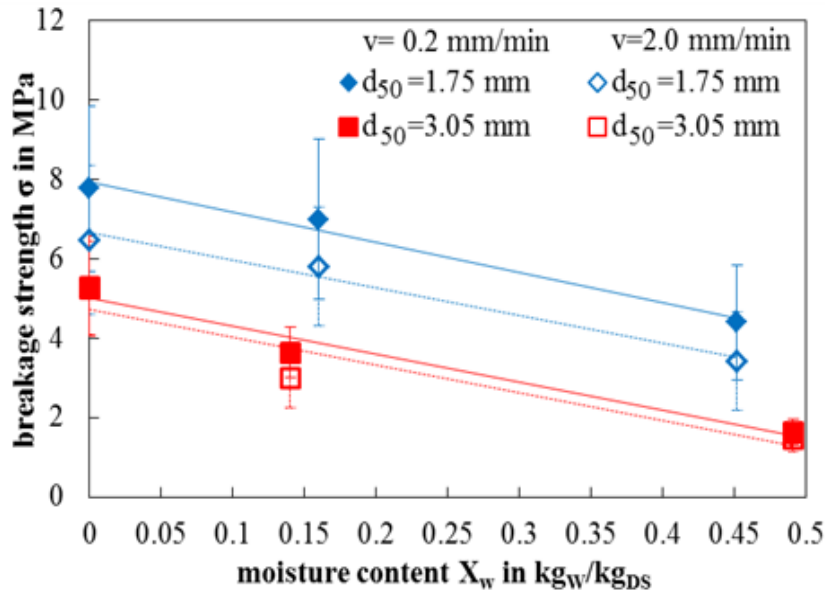
- significant decrease of k_{el} , E and p_y



Influence of loading velocity and moisture content:

- significant decrease of k_{el} , E and p_y with increasing loading velocity for moistened granules

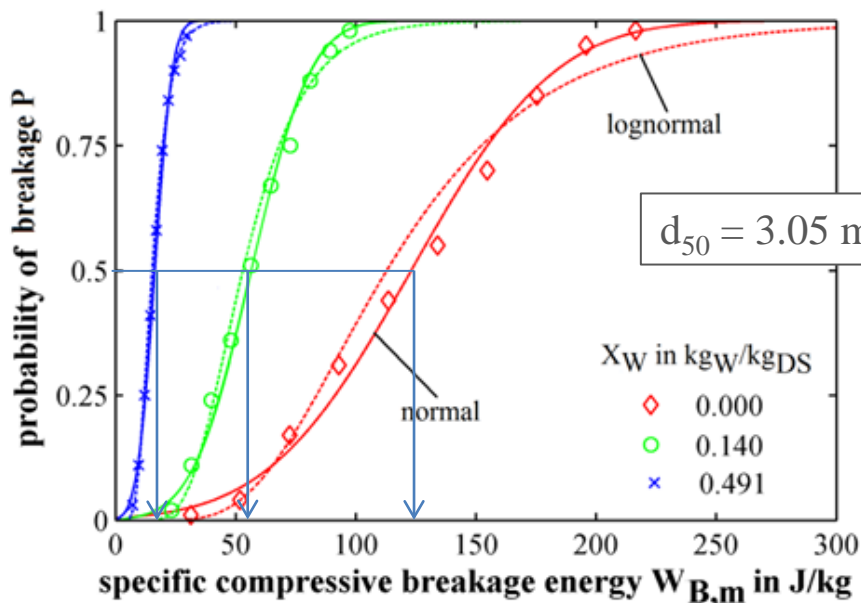
Breakage Characteristics of Fresh Granules



$$\sigma = \frac{F_B}{A_g} = \frac{4F_B}{\pi d^2}$$

Decrease of strength σ with:

- increasing granule size
- increasing loading velocity
- increasing moisture content

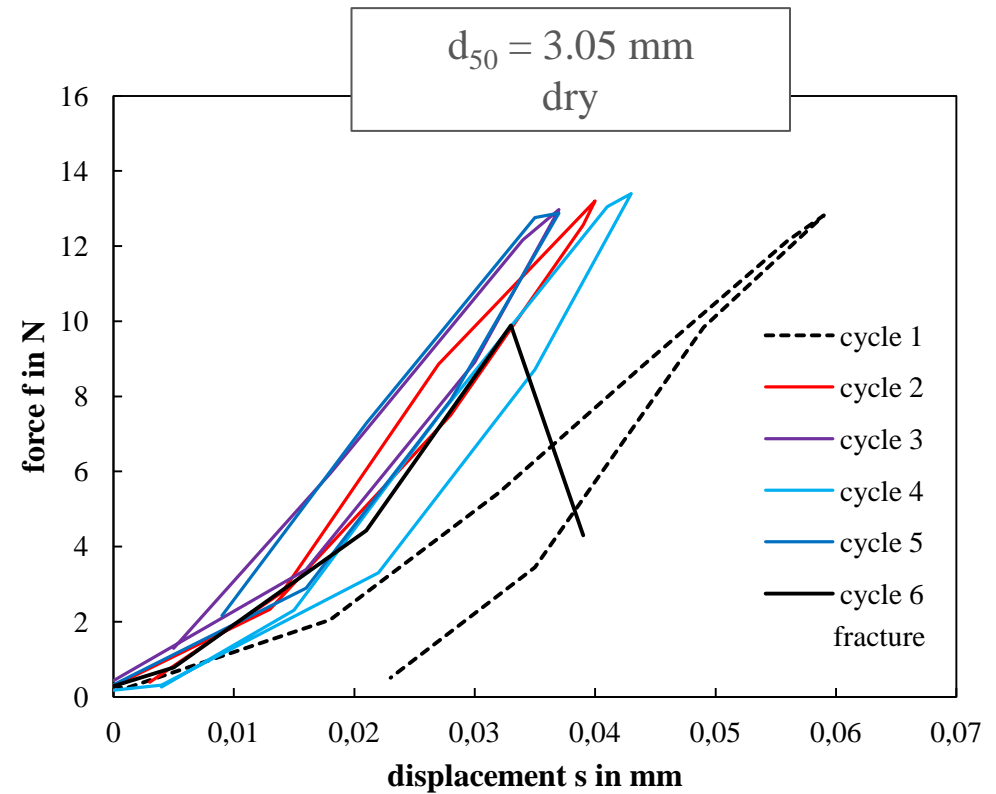


$$W_{B,m} = \frac{W_B}{m_g} = \frac{1}{m_g} \int_0^{s_B} F ds$$

$d_{50} = 3.05 \text{ mm}$	$W_{B,m,50}$
dry	130 J/kg
moist	58 J/kg
wet	22 J/kg

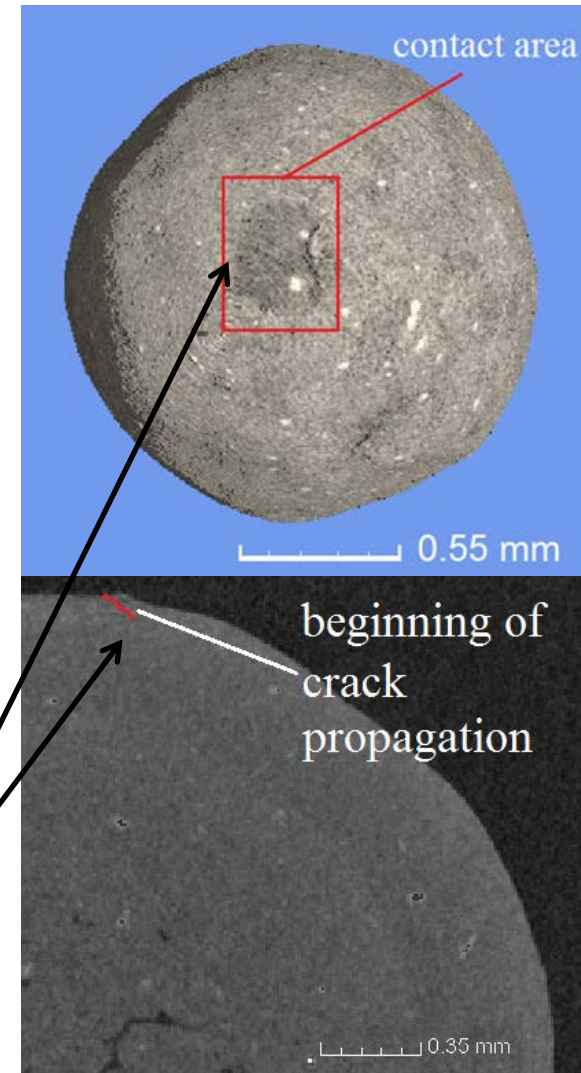
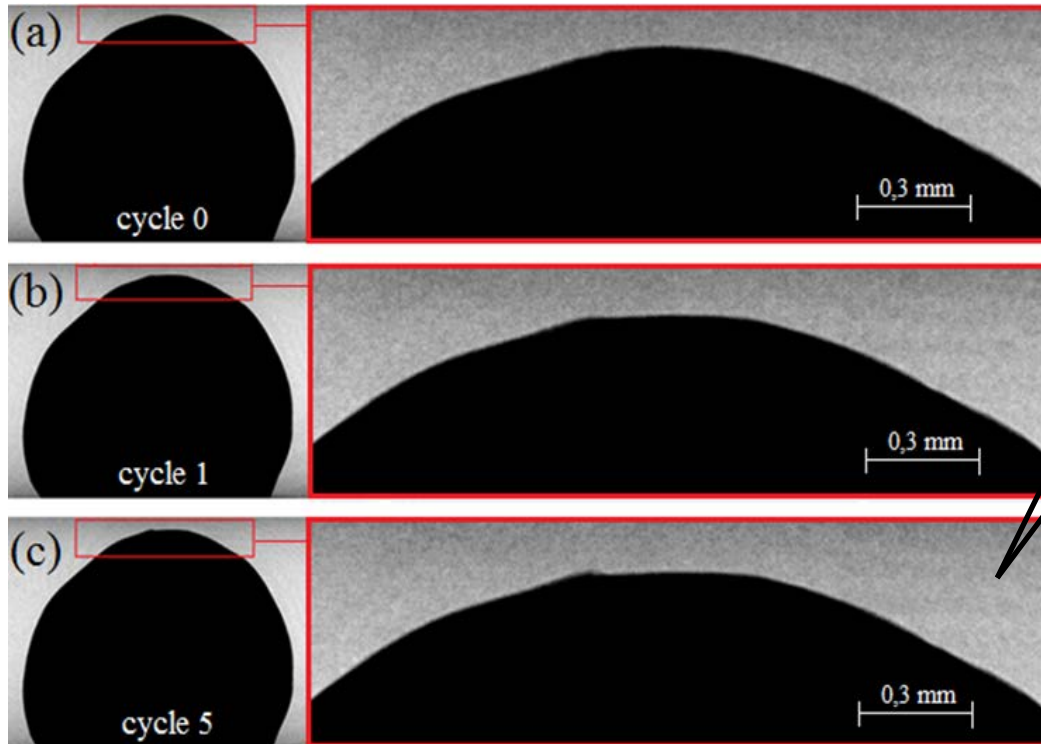
With increasing number of cycles:

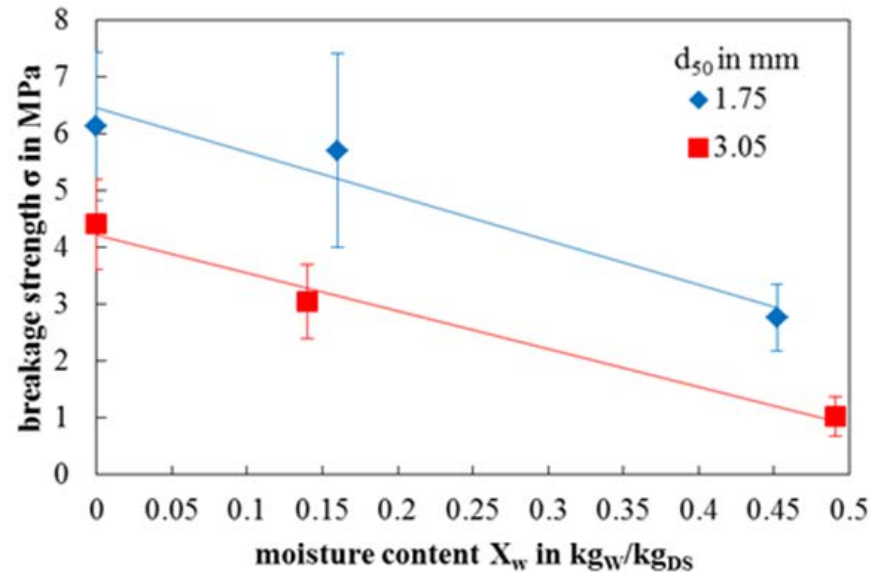
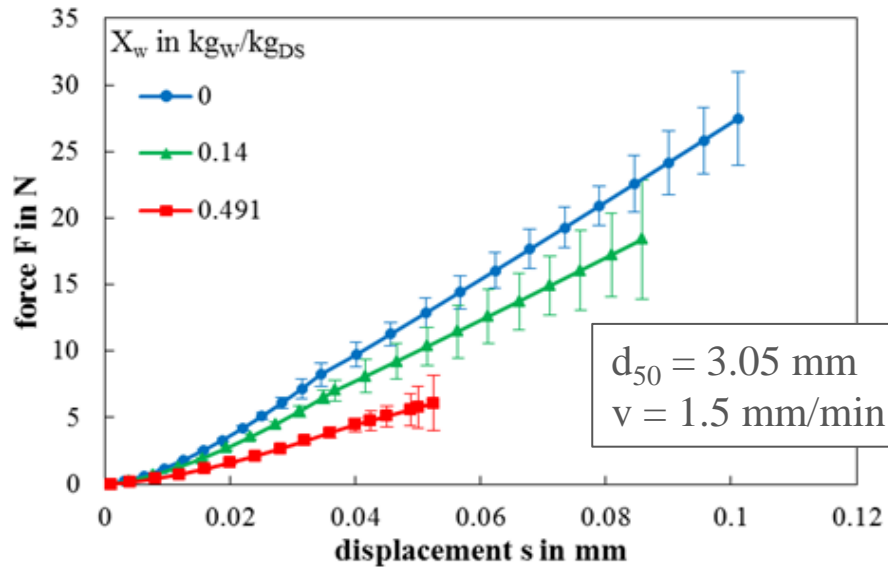
- decrease of plastic strain
- cyclic hardening effect:
 - increase of stiffness
 - significantly during first and second cycle
 - changes in microstructure promote breakage



Contact Flattening during Cyclic Loading

- dominant flattening of the curvature with increasing number of cycles
- visible denser elasto-plastically deformed area at the contact zone





With increasing moisture content:

- decrease of k_{el} , E and p_y
- decrease in displacement at breakage

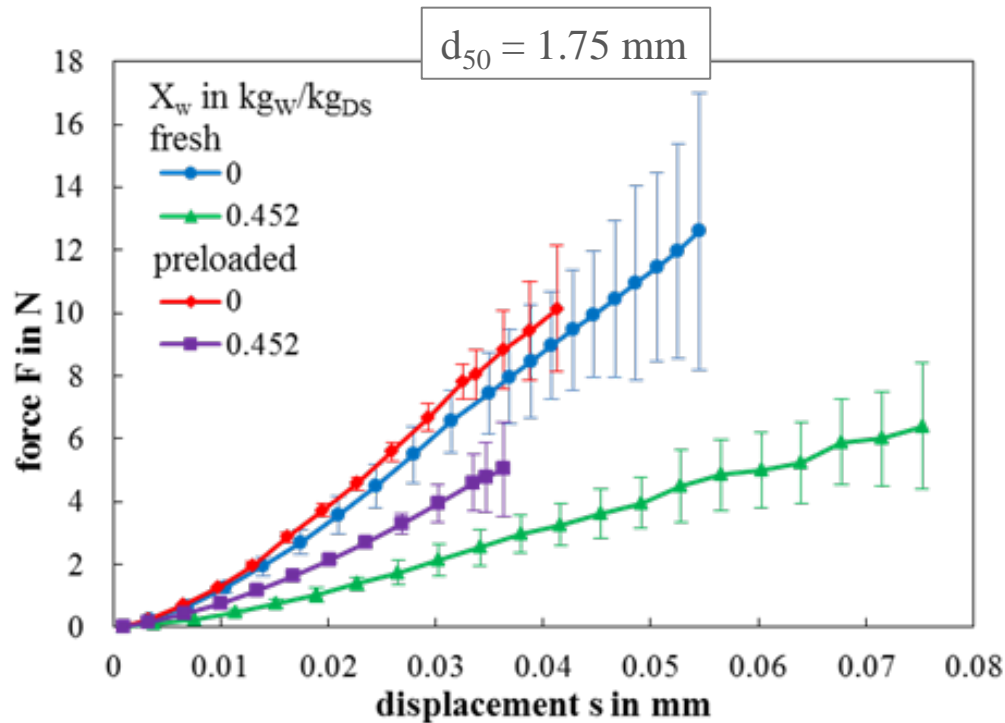
Breakage characteristics of preloaded granules:

Decrease of strength σ with :

- increasing granule size
- increasing moisture content

→ due to the damage of the inner granular structure

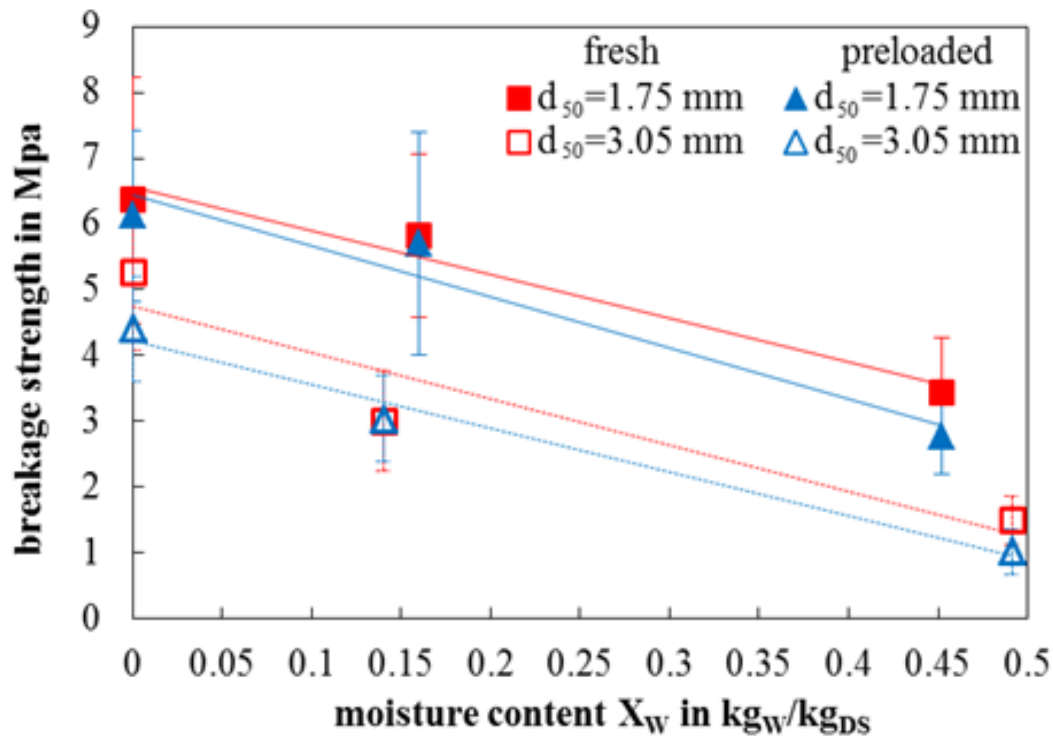
Comparison of the Material Behavior of Fresh and Preloaded Granules



Dry and completely wetted granules:

- increase of k_{el} , E and p_y with loading history (cyclic hardening effect)
- decrease in displacement at breakage, intensified with increasing moisture content

Comparison of Breakage Characteristics of Fresh and Preloaded Granuels



- decrease of breakage strength with loading history

State of the art before this thesis:

Influence of:

- granule size¹ larger → higher stiffness and lower strength
- loading velocity² faster → higher stiffness and lower strength
- moisture content³ wetter → lower stiffness and lower strength

What we didn't know:

- complex influence of loading velocity and moisture content
- influence of preloading
- crack propagation

1: Antonyuk, S., Ph.D. Thesis, Otto von Guericke University of Magdeburg (2006)

2: Russell, A., Müller, P., Shi, H., Tomas, J., AIChE Journal (2014)

3: Müller, P., Ph.D. Thesis, Otto von Guericke University of Magdeburg (2011)

State of the art now:

- influence of loading velocity and moisture content
 - with increasing loading velocity and moisture content:
lower stiffness and lower strength
- influence of preloading
 - higher stiffness
 - lower strength
- crack propagation according to Tomas^{1,2}

Future:

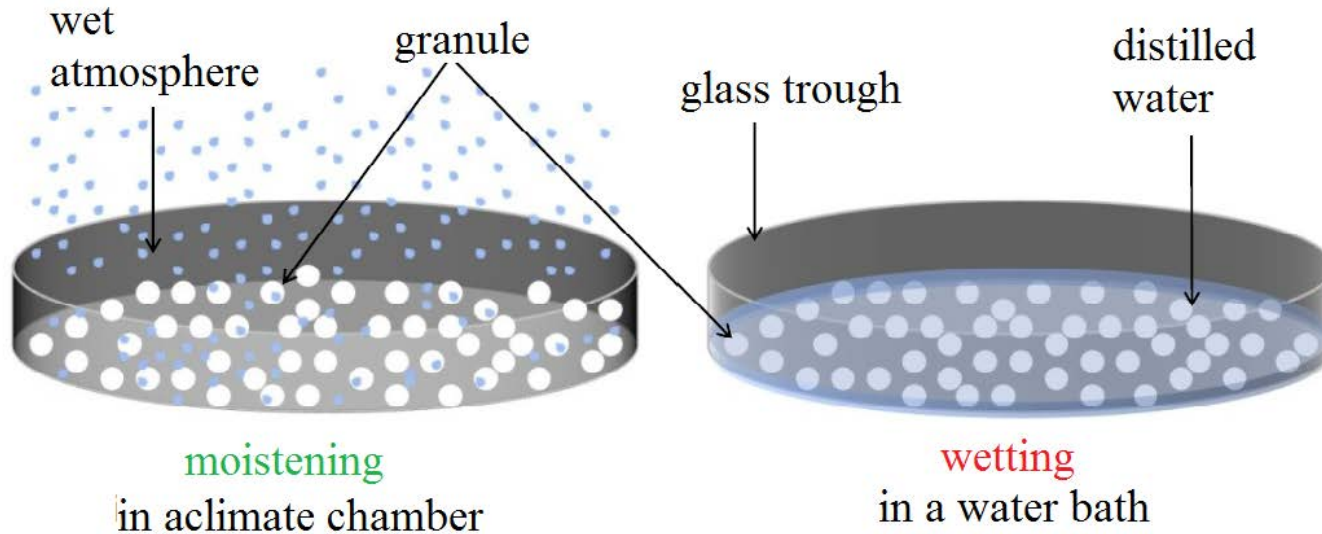
- creep tests
- influence of temperature

1: Tomas, J., Schreier, M., Gröger, T., Ehlers, S., Powder Technology 105, 39–51 (1999)

2: Tomas, J., Vorlesungsmanuskript, www.mvt.ovgu.de

Appendix

Zeolite 4AK



$$X_w = \frac{m_w}{m_{DS}} = \frac{m_{\text{tot}} - m_{DS}}{m_{DS}}$$

$$S = \frac{V_l}{V_{\text{pore}}} = \frac{(1 - \varepsilon)V_l}{\varepsilon V_s} = \frac{(1 - \varepsilon)\rho_s}{\varepsilon\rho_l} X_w$$

The force-displacement curve was well-fitted by:

- using the [Hertz model¹](#) for non-linear non-adhesive elastic loading

$$F_{\text{el,w-g-w}} = \frac{1}{6} E^* \sqrt{d_1} s^3 = \frac{1}{3} \frac{1}{(1-\nu_1^2)} E_1 \sqrt{d_1} s^3$$

$$k_{\text{el,w-g-w}} = \frac{dF_{\text{el,w-g-w}}}{ds} = \frac{1}{4} E^* \sqrt{d_1} s = \frac{1}{2} \frac{E_1}{(1-\nu_1^2)} \sqrt{d_1} s$$

- using the [Tomas model²](#) for non-linear non-adhesive elasto-plastic loading

$$F_{\text{el-pl,w-g-w}} = \pi \lambda_{\text{el-pl}} R_1 p_y \left(1 - \frac{1}{3} \sqrt[3]{\frac{s_y}{s}} \right) \frac{s}{2}$$

$$k_{\text{el-pl,w-g-w}} = \frac{dF_{\text{el-pl,w-g-w}}}{ds} = \pi \lambda_{\text{el-pl}} R_1 p_y \left(1 - \frac{2}{9} \sqrt[3]{\frac{s_y}{s}} \right)$$

1: Hertz, H., Journal für die reine und angewandte Mathematik 92, 156–171 (1882)

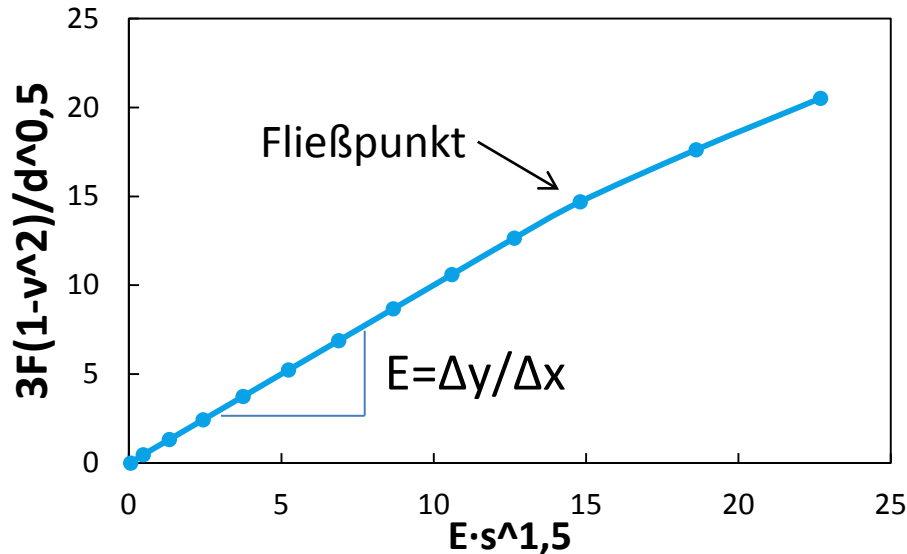
2: Tomas, J., Chem. Eng. Sci. 62, 1997–2010 (2007)

E - Modul

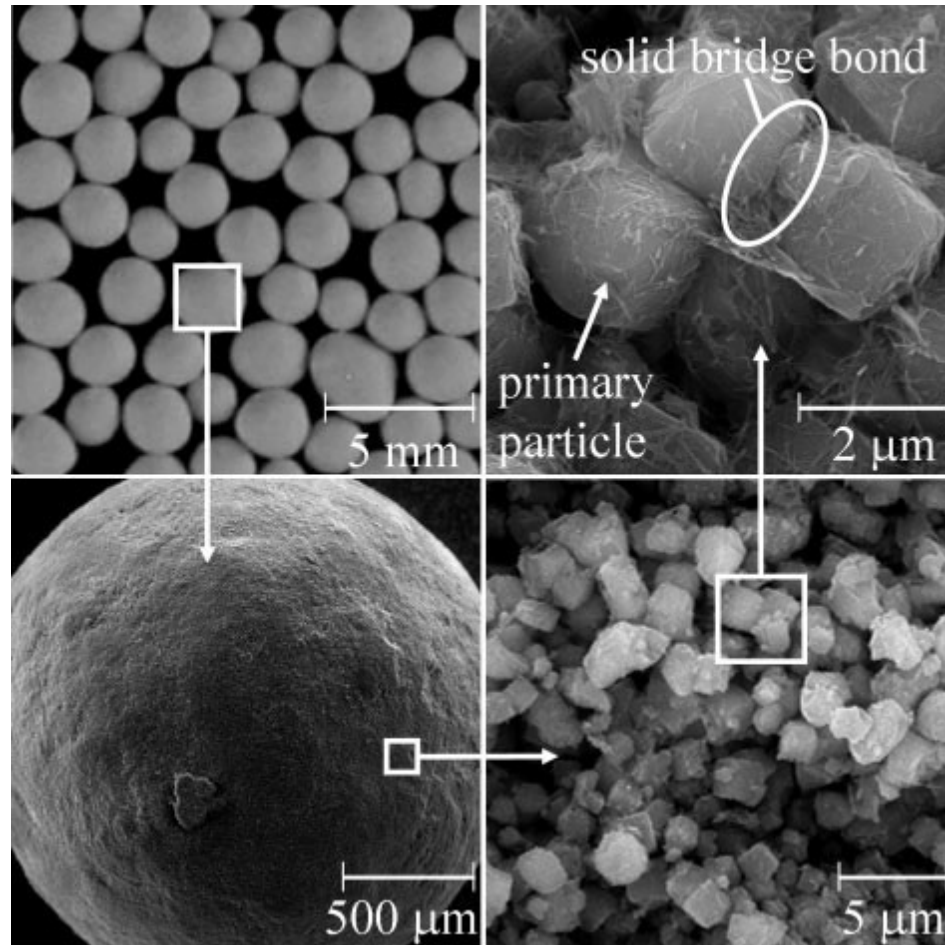
- Bestimmen des E – Modul durch Linearisierung des Hertz Modells

$$F_{\text{el,w-g-w}} = \frac{1}{3} \frac{1}{(1-\nu_1^2)} E_1 \sqrt{d_1} s^3 \xrightarrow{y = m \cdot x + n} 3F_{\text{el,w-g-w}} \cdot \frac{(1-\nu_1^2)}{d^{\frac{1}{2}}} = E_1 \cdot s^{\frac{3}{2}}$$

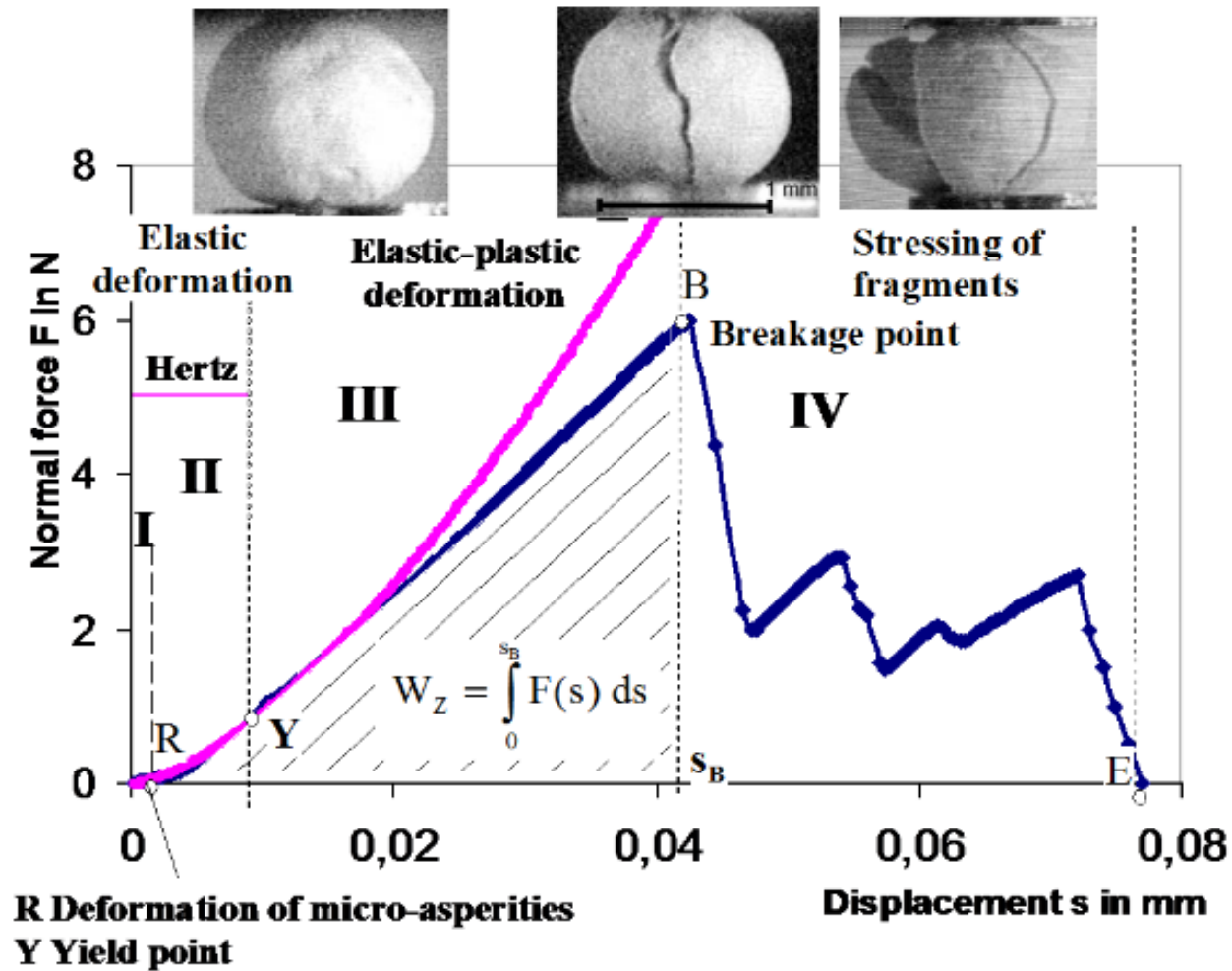
\uparrow
m



SEM Micrographs of the Granule Surface

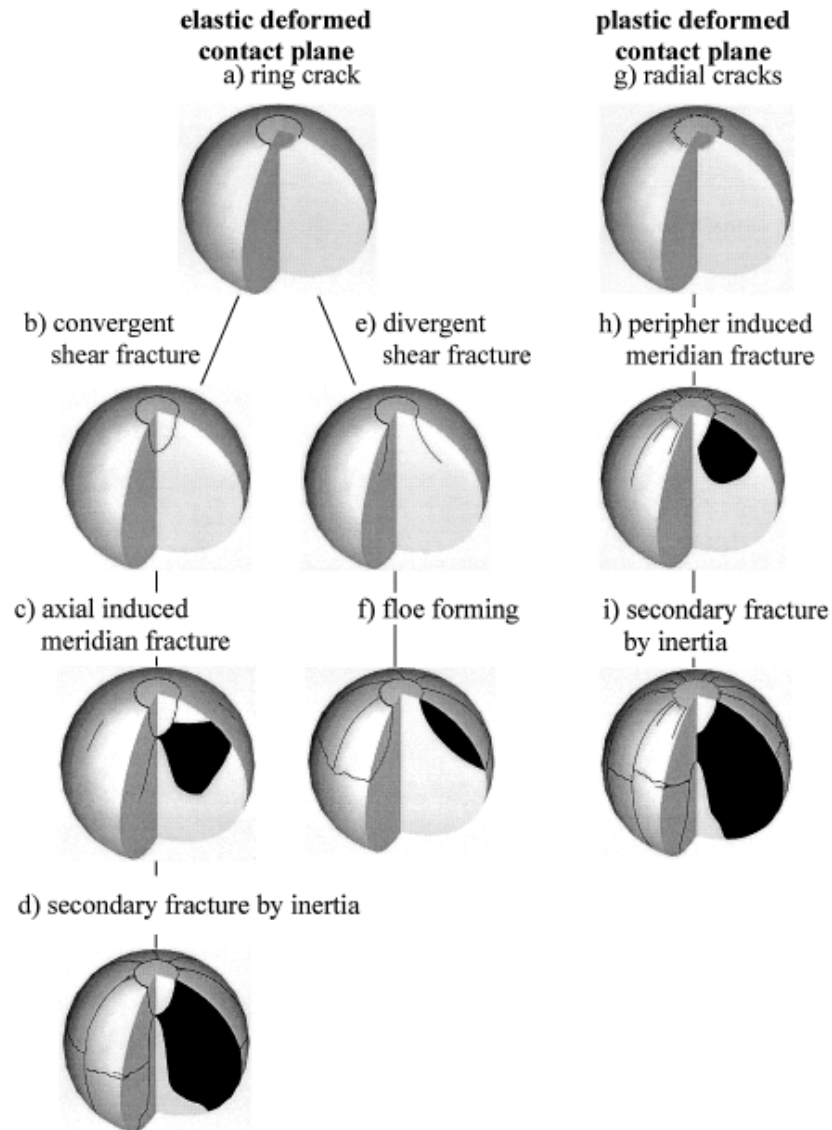


Crack Propagation

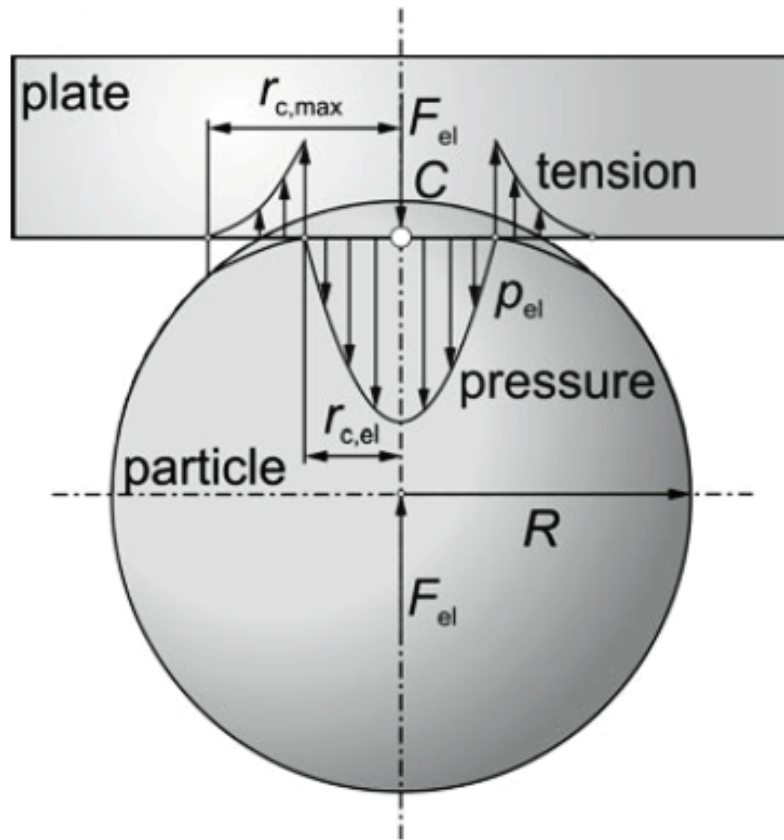


Source: Antonyuk, S., Ph.D. Thesis, Otto von Guericke University of Magdeburg (2006)
 Tomas, J., Vorlesungsmanuskript, www.mvt.ovgu.de

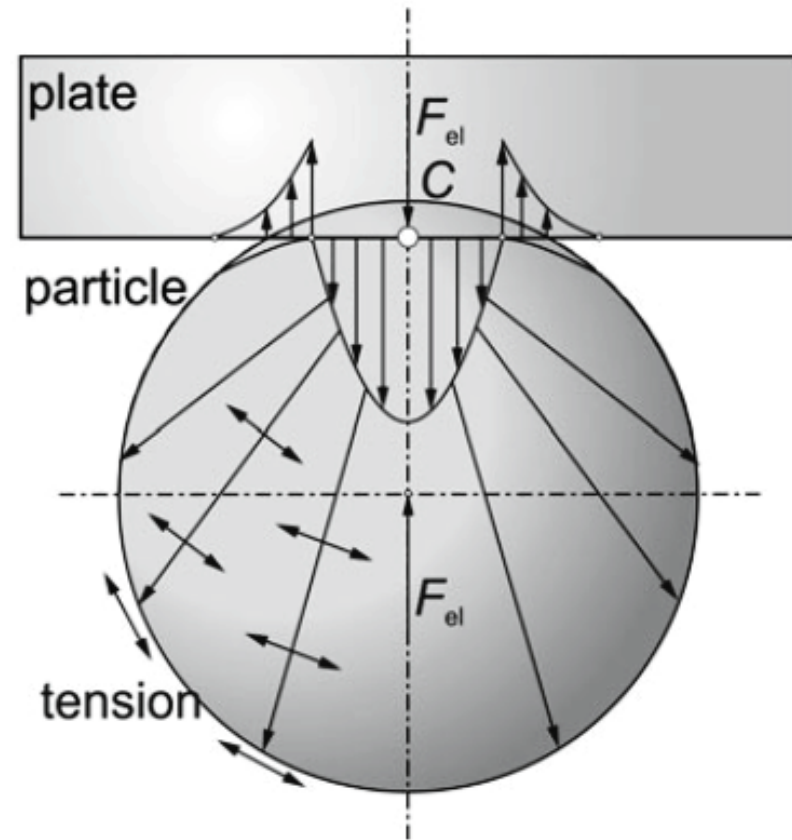
Crack Propagation



Comparison of the Stress State in Dry and Moist Granules

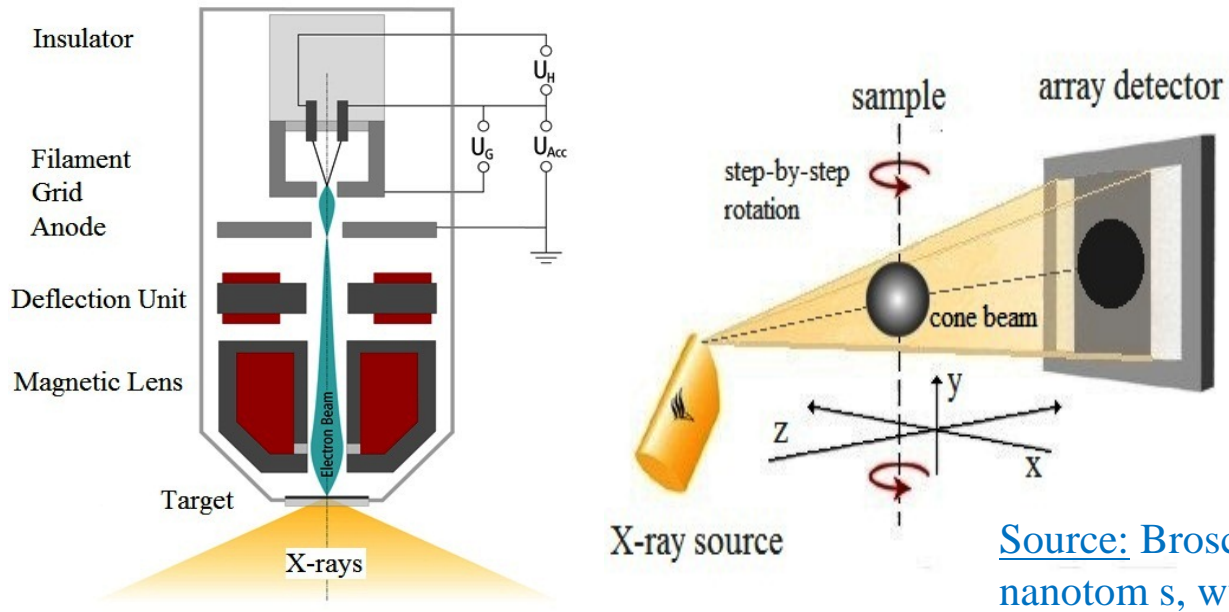


dry granule



moist granule

Micro CT and SEM



[Source: Broschure for phoenix nanotom s, www.ge-mcs.com](#)

